

A REGULAR RULE FOR GENERATION OF FULL CLASSES OF OPTIMAL SYSTEMS OF DF-SIGNALS BASED ON THE METHOD OF DECIMATION

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Based on the method of intrinsic decimation of an arbitrary sequence of different positive integers, where the sequence has the length p , a regular rule is suggested for generation of full classes of linear and nonlinear optimal systems of discrete frequency (DF) signals.

The methods of decimation and redecimation of M -sequences have many radio-engineering applications: investigation of structural properties of M -sequences [1–3]; generation of large ensembles of signals based on composite M -sequences [4]; treatment of the problem of obtaining different-in-structure (isomorphic) M -sequences without readjustment of feedback in a generator of M -sequences [5], etc.

The present work shows that the decimation method can be successfully used for construction of optimal systems of DF-signals permitting no more than a single coincidence [6].

The purpose of this work is to offer a regular rule for creating the full classes of linear and nonlinear optimal systems of DF-signals based on the method of decimation of an arbitrarily set sequence of p different positive integers, where p is a prime number.

Let the N -sequence be an arbitrary sequence of different natural numbers of length p having the form

$$N = \{n_1, n_2, \dots, n_i, \dots, n_p\} = \{n_i\}, i = \overline{1, p}, \quad (1)$$

where p is a prime number.

Definition 1. A sequence $D = \{n_{d,i}\}$, produced from $\{n_i\}$ by exclusion selection of the d th entries $i = \overline{1, p}$, is the result of decimation of N -sequence (1) in terms of the index d .

Obviously, the sequence D has the period p , since the greatest common divisor $(d, p) = 1$. The respective decimation is called intrinsic or normal [4]. These decimations are just the ones considered below.

Definition 2. By the frequency-time code based on decimation of an arbitrary N -sequence from (1), or D -code for brevity, is meant a set of code words defined by the rule

$$D = \begin{bmatrix} \{n_{1,i}\} \\ \{n_{2,i}\} \\ \vdots \\ \{n_{d,i}\} \\ \vdots \\ \{n_{(p-1),i}\} \end{bmatrix}, \quad i = \overline{1, p}. \quad (2)$$

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