

## METHODS FOR CONSTRUCTING COMPLETE FAMILIES OF 36-ELEMENT PERFECT BINARY ARRAYS

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**A new algorithm is developed for synthesis of two families of 36-element perfect binary arrays (6×6 and 3×12), and the completeness of both families is proved. A method is derived for constructing PBA of the format  $N/2 \times 2N$  with the aid of basic PBA of the format  $N \times N$  for any dimensionality  $N = 3 \cdot 2^n$ .**

With the advent of CDMA systems with multi-frequency carrier (MC-CDMA), there arises additional need in algorithms for construction of frequency-time signals with good auto- and cross-correlation properties. In this connection, of interest are perfect binary arrays (PBA), i.e., two-dimensional binary codes  $N_1 \times N_2$  with the ideal periodic autocorrelation function (PACF) in the form of delta function

$$R(0,0) = N_1 \times N_2, \quad R(u,v) = \sum_{i=0}^{N_1-1} \sum_{j=0}^{N_2-1} e_{i+u} e_{j+v} = 0$$

at any other  $u$  and  $v$ ,  $e_{ij} \in \{+1, -1\}$ .

One of fundamental properties of PBA is uniformity of their spectrum. Indeed, the two-dimensional discrete Fourier transform of the ideal PACF has the form

$$E_{kl}^2 = \sum_{u=0}^{N-1} \sum_{v=0}^{N-1} R(u,v) Z^{uk} Z^{vl} = \sum_{i,j=0}^{N-1} e_{ij} Z^{-(ik+jl)} \sum_{u,v=0}^{N-1} e_{uv} Z^{uk+vl} = E_{kl}^* \cdot E_{kl} = N^2,$$

where  $Z = Z_N = \exp(-2\pi j/N)$ .

There is a proof of existence of PBA of formats  $N \times N$  and  $N/2 \times 2N$  for dimensionality  $N = 2^n$  and  $N = 3 \cdot 2^n$ , where  $n$  is an integer [1, 2]. Procedures of construction of PBA for any  $N$  were deduced in [3], however, the method of synthesis of full classes of these arrays for  $N = 2^n$  was suggested only after elapse of ten years [4]. In [5] we can find a consistent substantiation of the method for construction of rectangular PBA of the format  $N/2 \times 2N$  from  $N \times N$  PBA.

In [6] the problem of synthesis of full classes of code sequences with length  $N$  and zero level of PACF at even shifts was handled based on alternation of pairs of complementary sequences of length  $N/2$ . It was natural to suggest a similar approach to synthesis of PBA from sets of four (quadruples) arrays with twice less dimensionality.

In [4] an  $N \times N$  PBA  $\mathbf{E}$  is formed by spatial alteration of elements  $\alpha$ ,  $\beta$ ,  $\gamma$ , and  $\delta$  of complementary  $N/2 \times 2N$  matrices  $\mathbf{A}$ ,  $\mathbf{B}$ ,  $\mathbf{C}$ , and  $\mathbf{D}$ , respectively, i.e.,

$$e_{2i,2j} = \alpha_{ij}; \quad e_{2i,2j+1} = \beta_{ij}; \quad e_{2i+1,2j} = \gamma_{ij}; \quad e_{2i+1,2j+1} = \delta_{ij},$$

or

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